

$$\begin{aligned}\sin x &= \frac{a}{c} = \cos\left(\frac{\pi}{2} - x\right) \\ &= \cos\left(x - \frac{\pi}{2}\right)\end{aligned}$$

choice B:  $\cos\left(x + \frac{\pi}{2}\right)$

$$\begin{aligned}&= -\cos\left(\pi - \left(x + \frac{\pi}{2}\right)\right) \\ &= -\cos\left(\frac{\pi}{2} - x\right)\end{aligned}$$

### Sine function transform

$$\left(T = \frac{2\pi}{\omega}\right)$$

↑

①  $A = 1$

period  $T = 1 - (-1 - 2\pi) = 2\pi \Rightarrow \omega = \frac{2\pi}{T} = 1$

The current function is obtained by moving  $y = \sin t$  to the right by 1.

$$\Rightarrow y = \sin(t - 1)$$

also correct:  $y = \sin(t - 1 + 2\pi)$

(if moving to the left, we move

$y = \sin t$  by a distance of  $2\pi - 1$ ,

then  $y = \sin(t + (2\pi - 1)) = \sin(t - 1 + 2\pi)$ )

## Sine function transform (cont'd)

[Try them before looking at the solutions here!]

(2)  $A = \frac{1}{\pi}$

period  $T = 3 - 1 = 2 \Rightarrow \omega = \frac{2\pi}{T} = \pi$

The function can be obtained by moving

$y = \frac{1}{\pi} \sin(\pi x)$  to the right by 1.

$\Rightarrow y = \frac{1}{\pi} \sin(\pi(x-1)) = \frac{1}{\pi} \sin(\pi x - \pi) = -\frac{1}{\pi} \sin(\pi x)$

↓  
Now look back at the graph. Indeed it's a flipped  $\frac{1}{\pi} \sin(\pi x)$  upside down.

(3)  $A = \frac{1}{2}$ .

period  $T = 2 \Rightarrow \omega = \frac{2\pi}{T} = \pi$

The function can be obtained by moving

$y = \frac{1}{2} \sin(\pi x)$  to the right by  $\frac{1}{2}$

$\Rightarrow y = \frac{1}{2} \sin(\pi(x - \frac{1}{2})) = \frac{1}{2} \sin(\pi x - \frac{\pi}{2})$

Alternatively, one can move  $\frac{1}{2} \cos(\pi x)$  to the right by 1.

Then  $y = \frac{1}{2} \cos(\pi(x-1)) = \frac{1}{2} \cos(\pi x - \pi) = \frac{1}{2} \sin(\pi x)$

$= -\frac{1}{2} \sin(\frac{\pi}{2} - (\pi x - \pi)) = -\frac{1}{2} \sin(-\pi x + \frac{3\pi}{2}) = \frac{1}{2} \sin(\pi x - \frac{\pi}{2})$

Sketch  $1 + 2\sin(2\pi x + 0.8\pi)$

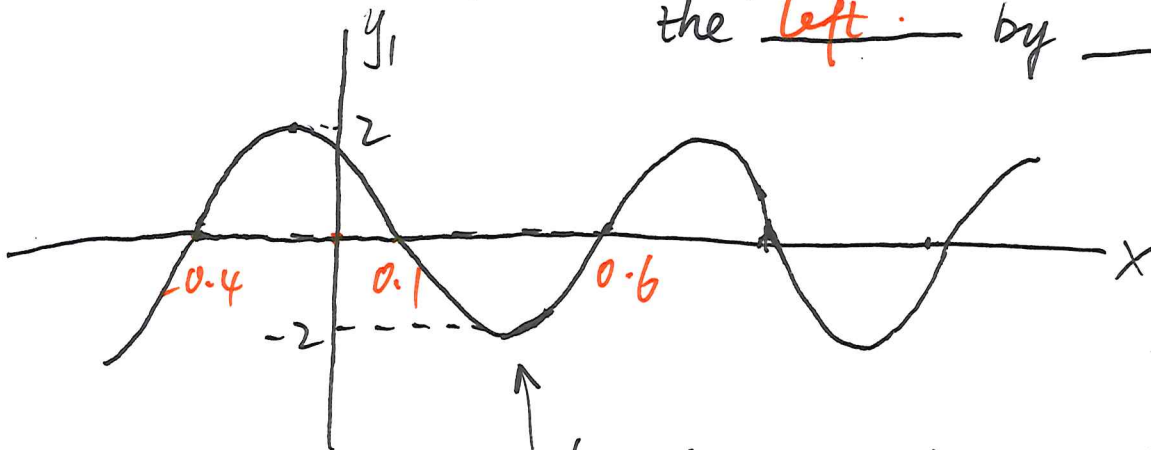
$$y = 2\sin(2\pi(x + 0.4)) + 1$$

First sketch  $y_1 = 2\sin(2\pi(x + 0.4))$

amplitude  $A = 2$

period  $T = \frac{2\pi}{2\pi} = 1$

$y_1$  is the function  $y_2 = 2\sin(2\pi x)$  moved to the left by 0.4.



sketch a complete period

Move  $y_1$  upward by 1

